Package: LearnGeom (via r-universe)

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Title Learning Plane Geometry

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Description Contains some functions to learn and teach basic plane Geometry at undergraduate level with the aim of being helpful to young students with little programming skills.

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Contents

`AddPointPoly` *Adds a point to a previously defined polygon*

Description

`AddPointPoly` creates a matrix to represent the polygon that connects several points

Usage

```
AddPointPoly(Poly, point, position)
```

Arguments

- `Poly` — Polygon object, previously created with function `CreatePolygon` or `CreateRegularPolygon`
- `point` — Vector containing the xy-coordinates of the point to be added to the polygon
- `position` — Integer indicating the position of the point in the original polygon, after which the new point is being added (considering that every polygon is an ordered list of points). It is convenient to visualize the polygon with `label = T` in order to avoid mistakes

Value

Returns a matrix which contains the points of the polygon. Each row represents one of the points

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
n <- 5
C <- c(0,0)
l <- 2
Penta <- CreateRegularPolygon(n, C, l)
Penta <- AddPointPoly(Penta, CenterPolygon(Penta), 1)
Draw(Penta, "blue", label = TRUE)
```

`Angle` *Computes the angle between three points*

Description

`Angle` computes the angle between three points

Usage

```
Angle(A, B, C, label = FALSE)
```

Arguments

- `A` — Vector containing the xy-cooydinates of point A
- `B` — Vector containing the xy-cooydinates of point B. This point acts as the vertex of angle ABC
- `C` — Vector containing the xy-cooydinates of point C
- `label` — Boolean. When `label = TRUE`, the plot displays the angle in the point that acts as the vertex. If missing, it works as with `label = FALSE`, so the angle is not displayed

Value

Angle between the three points in degrees

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
A <- c(-1,0)
B <- c(0,0)
C <- c(0,1)
Draw(CreatePolygon(A, B, C), "transparent")
angle <- Angle(A, B, C, label = TRUE)
angle <- Angle(A, C, B, label = TRUE)
angle <- Angle(B, A, C, label = TRUE)
```

CenterPolygon — *Computes the center of a given polygon. The center is obtained by averaging the x and y coordinates of the polygon*

Description

`CenterPolygon` computes the center of a polygon

Usage

```
CenterPolygon(Poly)
```

Arguments

`Poly`	Polygon object, previously created with either of the functions `CreatePolygon` or `CreateRegularPolygon`

Value

Vector which contains the xy-coordinates of the center of the polygon

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
C <- CenterPolygon(Poly)
x_min <- -5
x_max <- 5
y_min <- -5
```

```
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
Draw(Poly, "blue")
Draw(C, "red")
```

Circumcenter — *Computes the circumcenter of a given triangle, that is, the intersection of its three medians*

Description

`Circumcenter` computes the center of a triangle

Usage

```
Circumcenter(Tri, lines = F)
```

Arguments

`Tri`	Triangle object, previously created with function `CreatePolygon`
`lines`	Boolean. When `lines = TRUE`, the plot displays the lines that represent the medians of each of the sides of the triangle. If missing, it works as with `lines = FALSE`, so the lines are not displayed

Value

Vector which contains the xy-coordinates of the circumcenter of the triangle

References

http://mathworld.wolfram.com/Circumcenter.html

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Tri <- CreatePolygon(P1, P2, P3)
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
Draw(Tri, "transparent")
I <- Circumcenter(Tri, lines = TRUE)
Draw(I, "red")
```

`CoordinatePlane` *Plots an empty coordinate (cartesian) plane with customizable limits for the X and Y axis*

Description

`CoordinatePlane` plots an empty coordinate (cartesian) plane with customizable limits for the X and Y axis.

Usage

```
CoordinatePlane(x_min, x_max, y_min, y_max)
```

Arguments

`x_min`	Lowest value for the X axis
`x_max`	Highest value for the X axis
`y_min`	Lowest value for the Y axis
`y_max`	Highest value for the Y axis

Value

None. It produces a plot of a coordinate plane with axes and grid

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
```

`CreateArcAngles` *Creates an arc of a circumference*

Description

`CreateArcAngles` creates an arc of a circumference

Usage

```
CreateArcAngles(C, r, angle1, angle2, direction = "anticlock")
```

Arguments

`C`	Vector containing the xy-coordinates of the center of the circumference
`r`	Radius for the circumference (or arc)
`angle1`	- Angle in degrees (0-360) at which the arc starts
`angle2`	- Angle in degrees (0-360) at which the arc finishes
`direction`	- String indicating the direction which is considered to create the arc, from the smaller to the higher angle. It has two possible values: "clock" (clockwise direction) and "anticlock" (anti-clockwise direction)

Value

Returns a vector which contains the center, radius, angles (0-360) and direction (1 - "clock", 2 - "anticlock") that define the created arc

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
C <- c(0,0)
r <- 3
angle1 <- 90
angle2 <- 180
direction <- "anticlock"
Arc1 <- CreateArcAngles(C, r, angle1, angle2, direction)
Draw(Arc1, "black")
direction <- "clock"
Arc2 <- CreateArcAngles(C, r, angle1, angle2, direction)
Draw(Arc2, "red")
```

`CreateArcPointsDist` *Creates an arc of a circumference to connect two points*

Description

`CreateArcPointsDist` creates an arc of a circumference to connect two points

Usage

```
CreateArcPointsDist(P1, P2, r, choice, direction)
```

Arguments

- `P1` Vector containing the xy-coordinates of point 1
- `P2` Vector containing the xy-coordinates of point 2
- `r` Radius for the circumference which is used to generate the arc. This parameter is necessary because there are infinite possible arcs that connect two points. In the case the radius is smaller than half the distance between `P1` and `P2`, there is no possible arc, so the function tells the user
- `choice` - Integer indicating which of the two possible centers is chosen to create the arcs. A value of 1 means the center of the circle that contains the arc is chosen in the direction of M + v, being M the middle point between P1 and P2 and v the orthogonal vector of P2 - P1 normalized to the appropriate length for creating the desired arc. A value of 2 means the center of the resulting circle is chosen in the direction of M - V. Remark: There are as well two options for vector v. If P1 = (a,b) and P2 = (c,d), v is written in the internal function as (b-d,c-a)
- `direction` - String indicating the direction which is considered to create the arc, from the smaller to the higher angle. It has two possible values: "clock" (clockwise direction) and "anticlock" (anti-clockwise direction)

Value

Returns a vector which contains the center, radius and angles (0-360) that define the created arc

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(-3,2)
P2 <- c(0,0)
r <- sqrt(18)/2
choice=1
direction="anticlock"
Arc <- CreateArcPointsDist(P1, P2, r, choice, direction)
Draw(Arc, "red")
choice=2
direction="anticlock"
Arc <- CreateArcPointsDist(P1, P2, r, choice, direction)
Draw(Arc, "blue")
choice=1
direction="clock"
Arc <- CreateArcPointsDist(P1, P2, r, choice, direction)
Draw(Arc, "pink")
choice=2
direction="clock"
Arc <- CreateArcPointsDist(P1, P2, r, choice, direction)
Draw(Arc, "green")
```

`CreateLineAngle` *Creates a vector to represent a line that passes through a point and forms certain angle with X axis*

Description

`CreateLineAngle` creates a vector to represent a line that passes through a point and forms certain angle with X axis

Usage

```
CreateLineAngle(P, angle)
```

Arguments

`P`	Vector containing the xy-coordinates of a point
`angle`	Angle in degrees (0-360) for the line

Value

Returns a vector which contains the slope and intercept of the defined line. If the angle is defined as 90, the slope is set to `Inf` and the intercept is replaced by the x-value for the line (which is a vertical line in this situation)

Examples

```
P <- c(0,0)
angle <- 45
Line <- CreateLineAngle(P, angle)
```

`CreateLinePoints` *Creates a vector that represents the line that connects two points*

Description

`CreateLinePoints` creates a vector that represents the line that connects two points

Usage

```
CreateLinePoints(P1, P2)
```

Arguments

`P1`	Vector containing the xy-coordinates of point 1
`P2`	Vector containing the xy-coordinates of point 2

Value

Returns a vector which contains the slope and intercept of the defined line. If the points have the same x-coordinate, the slope is set to `Inf` and the intercept is replaced by the x-value for the line (which is a vertical line in this situation)

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
Line <- CreateLinePoints(P1, P2)
```

CreatePolygon *Creates a matrix to represent the polygon that connects several points*

Description

`CreatePolygon` creates a matrix to represent the polygon that connects several points

Usage

```
CreatePolygon(...)
```

Arguments

`...`	An undetermined number of points introduced by the user in the form of vectors

Value

Returns a matrix which contains the points of the polygon. Each row represents one of the points

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
```

`CreateRegularPolygon` *Creates a matrix to represent a regular polygon*

Description

`CreateRegularPolygon` creates a matrix to represent the polygon that connects several points

Usage

```
CreateRegularPolygon(n, C, l)
```

Arguments

`n`	Number of sides for the polygon
`C`	Vector containing the xy-coordinates for the center of the regular polygon
`l`	Length of the sides for the polygon

Value

Returns a matrix which contains the points of a regular polygon given its number of points and the length of its sides. Each row represents one of the points

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
n <- 5
C <- c(0,0)
l <- 1
Penta <- CreateRegularPolygon(n, C, l)
Draw(Penta, "blue", label = TRUE)
```

`CreateSegmentAngle` *Creates a matrix that represents the segment that starts from a point with certain length and angle*

Description

`DrawSegment` plots the segment that connects two points in a previously generated coordinate plane

Usage

```
CreateSegmentAngle(P, angle, l)
```

Arguments

P	Vector containing the xy-coordinates of the point
angle	Angle in degrees (0-360) for the segment
l	Positive number that indicates the length for the segment

Value

Returns a matrix which contains the points that determine the extremes of the segment

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P <- c(0,0)
angle <- 30
l <- 1
Segment <- CreateSegmentAngle(P, angle, l)
Draw(Segment, "black")
```

CreateSegmentPoints *Creates a matrix that represents the segment that connects two points*

Description

`DrawSegment` plots the segment that connects two points in a previously generated coordinate plane

Usage

```
CreateSegmentPoints(P1, P2)
```

Arguments

P1	Vector containing the xy-coordinates of point 1
P2	Vector containing the xy-coordinates of point 2

Value

Returns a matrix which contains the points that determine the extremes of the segment

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(0,0)
P2 <- c(1,1)
Segment <- CreateSegmentPoints(P1, P2)
Draw(Segment, "black")
```

`DistanceLines` *Computes the distance between two lines*

Description

`DistanceLines` computes the distance between two lines

Usage

```
DistanceLines(Line1, Line2)
```

Arguments

`Line1`	Line object previously created with `CreateLinePoints` or `CreateLineAngle`
`Line2`	Line object previously created with `CreateLinePoints` or `CreateLineAngle`

Value

Returns the distance between two points

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
Line1 <- CreateLinePoints(P1, P2)
P3 <- c(1,-1)
P4 <- c(2,0)
Line2 <- CreateLinePoints(P3, P4)
d <- DistanceLines(Line1, Line2)
```

`DistancePointLine` *Computes the distance between a point and a line*

Description

`DistancePointLine` computes the distance between a point and a line

Usage

```
DistancePointLine(P, Line)
```

Arguments

`P`	Vector containing the xy-coordinates of a point
`Line`	Vector object previously created with `CreateLinePoints` or `CreateLineAngle`

Value

Returns the distance between a point and a line. This distance corresponds to the distance between the point and its orthogonal projection into the line

Examples

```
P <- c(2,1)
P1 <- c(0,0)
P2 <- c(1,1)
Line <- CreateLinePoints(P1, P2)
d <- DistancePointLine(P, Line)
```

`DistancePoints` *Computes the distance between two points*

Description

`DistancePoints` computes the distance between two points

Usage

```
DistancePoints(P1, P2)
```

Arguments

`P1`	Vector containing the xy-coordinates of point 1
`P2`	Vector containing the xy-coordinates of point 2

Value

Returns the euclidean distance between two points

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
d <- DistancePoints(P1, P2)
```

`Draw` *Plots a geometric object*

Description

`Draw` plots geometric objects

Usage

```
Draw(object, colors = c("black", "black"), label = FALSE)
```

Arguments

`object`	geometric object of any of these five types: point, segment, arc, line or polygon. A point is simply a vector of length 2, which contains the xy-coordinates for the point. For the other four types, there can be created with any of the following functions: - `CreateArcAngles` - `CreateArcPointsDist` - `CreateLineAngle` - `CreateLinePoints` - `CreatePolygon` - `CreateRegularPolygon` - `CreateSegmentAngle` - `CreateSegmentPoints`
`colors`	Vector containing information about the color for the object to be plotted. In the case of polygons, the vector should have length 2 to define the background color and the border color (in this order). Moreover, it can be used `"transparent"` in the case no background color is needed for the polygon. For the other four types of objects, `color` should be a vector of length 1 (or a simple string) to indicate the color for the object. If this parameter is not specified the default color is black (for polygons, it is black for the background and the border)
`label`	Boolean, only used for polygons. When `label = TRUE` and the object is a polygon, the plot displays the numbers that correspond to the order of the points of the polygon. If missing, it works as with `label = FALSE`, so the numbers are not displayed

Value

None. It produces the plot of a geometric object (point, segment, arc, line or polygon) in the current coordinate plane

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
Draw(Poly, c("blue"))
```

Duopoly — *Plots a fractal curve from the trochoids family. Any curve from this family can be defined by some parametrical equations, but they can also be produced (approximated) through a simple iterative process based on segment drawing for certain angles and lengths*

Description

`Duopoly` plots a closed curve from the trochoids family

Usage

```
Duopoly(P, l1, angle1, l2, angle2, time = 0, color = "transparent")
```

Arguments

`P`	Vector containing the xy-coordinates of the starting point for the curve
`l1`	Number that indicates the length side of the segment drawn the first in each of the steps of the process
`angle1`	Angle (0-360) that indicates the direction of the segment which is drawn the first in each of the steps of the process
`l2`	Number that indicates the length side of the segment drawn the second in each of the steps of the process
`angle2`	Angle (0-360) that indicates the direction of the segment which is drawn the second in each of the steps of the process
`time`	Number of seconds to wait for the program before drawing each of the segments that make the trochoid curve. If no `time` is specified, default value is 0 (no waiting time). If the chosen time is very small (`time` < 0.05) it is possible that the program shows the plot directly. In this case, it should be increased the `time` parameter.

color — Color to indicate the points that are obtained during the process to approximate the trochoid. If missing, the points are not indicated and only the segments are drawn in the plot

Value

None. It produces the plot of a curve from the trochoids family

References

Abelson, H., & DiSessa, A. A. (1986). Turtle geometry: The computer as a medium for exploring mathematics. MIT press

Armon, U. (1996). Representing trochoid curves by DUOPOLY procedure. International Journal of Mathematical Education in Science and Technology, 27(2), 177-187

Examples

```
x_min <- -100
x_max <- 100
y_min <- -50
y_max <- 150
CoordinatePlane(x_min, x_max, y_min, y_max)
P <- c(0,0)
l1 <- 2
angle1 <- 3
l2 <- 2
angle2 <- 10
Duopoly(P, l1, angle1, l2, angle2)
```

FractalSegment — *Plots a fractal curve starting from a segment*

Description

`FractalSegment` plots the first iterations of a fractal curve, starting from a segment in the plane

Usage

```
FractalSegment(P1, P2, angle, cut1, cut2, f, it)
```

Arguments

P1 — Vector containing the xy-coordinates of point 1. This point is the left extreme of the segment that corresponds to the first iteration (`it` = 1)

P2 — Vector containing the xy-coordinates of point 2. This point is the right extreme of the segment that corresponds to the first iteration (`it` = 1)

angle — Angle (0-360) that determines the angle with which the new segments are drawn at the cut points

cut1	Number bigger than 0 and smaller than 1 that indicates the proportional part of the segment at which the first cut occurs. This parameter determines the position of the first cut point
cut2	Number bigger than 0 and smaller than 1 that indicates the proportional part of the segment at which the second cut occurs. This parameter determines the position of the second cut point
f	Positive number that produces an enlargement or a reduction for the new drawn segment in each iteration
it	Number of iterations to be performed for the construction of the fractal curve. It is not recommended to choose a number higher than 7 in order to avoid an excess of computation

Value

None. It produces the plot of the first `n` iterations of a fractal curve in the current coordinate plane. The choice of parameters `cut1 = 1/3`, `cut2 = 2/3`, `angle = 60` and `f = 1` produces the Koch curve

References

http://mathworld.wolfram.com/Fractal.html

Examples

```
x_min <- -6
x_max <- 6
y_min <- -4
y_max <- 8
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(-5,0)
P2 <- c(5,0)
angle <- 90
cut1 <- 1/3
cut2 <- 2/3
f <- 1
it <- 4
FractalSegment(P1, P2, angle, cut1, cut2, f, it)
```

Homothety — *Creates an homothety from a given polygon*

Description

`Homothety` creates an homothety from a given polygon

Usage

```
Homothety(Poly, C, k, lines = F)
```

Arguments

`Poly`	Polygon object, previously created with function `CreatePolygon`
`C`	Vector containing the xy-coordinates of the center of the homothety
`k`	Number which represents the expansion or contraction factor for the homothety
`lines`	Boolean. When `lines = TRUE`, the plot displays the lines that connect the center of the homothety with the points of the polygons (the original and the transformed one). If missing, it works as with `lines = FALSE`, so the lines are not displayed

Value

Returns the coordinates of a polygon that has been transformed according to the homothethy with center at `C` and factor `k`

References

https://www.encyclopediaofmath.org/index.php/Homothety

Examples

```
x_min <- -2
x_max <- 6
y_min <- -3
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
Draw(Poly, "blue")
C <- c(-1,-2)
k1 <- 0.5
Poly_homothety1 <- Homothety(Poly, C, k1, lines = TRUE)
Draw(Poly_homothety1, "orange")
k2 <- 2
Poly_homothety2 <- Homothety(Poly, C, k2, lines = TRUE)
Draw(Poly_homothety2, "orange")
```

`Incenter` *Computes the incenter of a given triangle*

Description

`Incenter` computes the center of a triangle

Usage

```
Incenter(Tri, lines = F)
```

Arguments

`Tri`	Triangle object, previously created with function `CreatePolygon`
`lines`	Boolean. When `lines = TRUE`, the plot displays the lines that bisect each of the angles of the triangle. If missing, it works as with `lines = FALSE`, so the lines are not displayed

Value

Vector which contains the xy-coordinates of the incenter of the triangle

References

http://mathworld.wolfram.com/Incenter.html

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Tri <- CreatePolygon(P1, P2, P3)
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
Draw(Tri, "transparent")
I <- Incenter(Tri, lines = TRUE)
Draw(I, "red")
```

IntersectLineCircle *Finds the intersection between a line and a circumference*

Description

`IntersectLineCircle` finds the intesection between a line and a circumference

Usage

```
IntersectLineCircle(Line, C, r)
```

Arguments

`Line`	Line object previously created with `CreateLinePoints` or `CreateLineAngle`
`C`	Vector containing the xy-coordinates of the center of the circumference
`r`	Radius for the circumference

Value

Returns a vector containing the xy-coordinates of the intersection points. In case of no intersection, the function tells the user

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
Line <- CreateLinePoints(P1, P2)
C <- c(0,0)
r <- 2
intersection <- IntersectLineCircle(Line, C, r)
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
Draw(Line, "black")
Draw(CreateArcAngles(C, r, 0, 360), "black")
Draw(intersection[1,], "red")
Draw(intersection[2,], "red")
```

`IntersectLines` *Finds the intersection of two lines*

Description

`IntersectLines` finds the intesection of two lines

Usage

```
IntersectLines(Line1, Line2)
```

Arguments

`Line1`	Line object previously created with `CreateLinePoints` or `CreateLineAngle`
`Line2`	Line object previously created with `CreateLinePoints` or `CreateLineAngle`

Value

Returns a vector containing the xy-coordinates of the intersection point. In case of no intersection, the function tells the user

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
Line1 <- CreateLinePoints(P1, P2)
P3 <- c(1,-1)
P4 <- c(2,0)
Line2 <- CreateLinePoints(P3, P4)
intersection <- IntersectLines(Line1, Line2)
```

Koch *Plots the Koch curve*

Description

Koch plots the first iterations of Koch curve, a well-known fractal

Usage

```
Koch(P1, P2, it)
```

Arguments

P1	Vector containing the xy-coordinates of point 1. This point is the left extreme of the segment that corresponds to the first iteration (it = 1)
P2	Vector containing the xy-coordinates of point 2. This point is the right extreme of the segment that corresponds to the first iteration (it = 1)
it	Number of iterations to be performed for the construction of Koch curve. It is not recommended to choose a number higher than 7 in order to avoid an excess of computation

Value

None. It produces the plot of the first n iterations of Koch curve in the current coordinate plane

References

http://mathworld.wolfram.com/KochSnowflake.html

Examples

```
x_min <- -6
x_max <- 6
y_min <- -4
y_max <- 8
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(-5,0)
P2 <- c(5,0)
it <- 4
Koch(P1, P2, it)
```

LinesAngles — *Computes the angle that form two lines*

Description

LinesAngles computes the angle that form two lines

Usage

```
LinesAngles(Line1, Line2)
```

Arguments

Line1	Line object previously created with CreateLinePoints or CreateLineAngle
Line2	Line object previously created with CreateLinePoints or CreateLineAngle

Value

Returns the angle that form the two lines

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
Line1 <- CreateLinePoints(P1, P2)
P3 <- c(1,-1)
P4 <- c(2,3)
Line2 <- CreateLinePoints(P3, P4)
angle <- LinesAngles(Line1, Line2)
```

MidPoint — *Computes the middle point of the segment that connects two points*

Description

MidPoint computes the middle point of the segment that connects two points

Usage

```
MidPoint(P1, P2)
```

Arguments

P1	Vector containing the xy-coordinates of point 1
P2	Vector containing the xy-coordinates of point 2

Value

Returns a vector containing the xy-coordinates of the middle point of the segment that connects `P1` and `P2`

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
mid <- MidPoint(P1, P2)
```

`PolygonAngles` *Computes each of the existing angles in a given polygon*

Description

`PolygonAngles` computes each of the existing angles in a given polygon

Usage

```
PolygonAngles(Poly)
```

Arguments

`Poly`	Polygon object, previously created with function `CreatePolygon`

Value

Returns a vector containing the angles for each of the points of a polygon. The resulting vector follows the order of the points in the defined polygon

Examples

```
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
angles <- PolygonAngles(Poly)
```

`ProjectPoint` *Computes the orthogonal projection of a point onto a line*

Description

`ProjectPoint` computes the orthogonal projection of a point onto a line

Usage

```
ProjectPoint(P, Line)
```

Arguments

`P`	Vector containing the xy-coordinates of a point
`Line`	Line object previously created with `CreateLinePoints` or `CreateLineAngle`, to be used as the axis of symmetry

Value

Returns a vector which contains the xy-coordinates of the projection point

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
xx <- c(0,1,2)
yy <- c(0,1,0)
P1 <- c(0,0)
P2 <- c(1,1)
Line <- CreateLinePoints(P1, P2)
Draw(Line, "black")
P <- c(-2,2)
Draw(P, "black")
projection <- ProjectPoint(P, Line)
Draw(projection, "red")
```

ReflectedPoint *Computes the reflected point about a line of a given point*

Description

ReflectedPoint computes the reflected point about a line of a given point

Usage

```
ReflectedPoint(P, Line)
```

Arguments

P	Vector containing the xy-coordinates of a point
Line	Line object previously created with CreateLinePoints or CreateLineAngle, to be used as the axis of symmetry

Value

Returns a vector which contains the xy-coordinates of the reflected point

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
xx <- c(0,1,2)
yy <- c(0,1,0)
P1 <- c(0,0)
P2 <- c(1,1)
Line <- CreateLinePoints(P1, P2)
Draw(Line, "black")
P <- c(-2,2)
Draw(P, "black")
reflected <- ReflectedPoint(P, Line)
Draw(reflected, "red")
```

`ReflectedPolygon` *Creates the reflection about a line of a given polygon*

Description

`ReflectedPolygon` creates the reflection about a line of a given polygon

Usage

```
ReflectedPolygon(Poly, Line)
```

Arguments

`Poly`	Polygon object, previously created with function `CreatePolygon` or `CreateRegularPolygon`
`Line`	Line object previously created with `CreateLinePoints` or `CreateLineAngle`, to be used as the axis of symmetry

Value

Returns the reflection of a polygon about a line

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
Draw(Poly, "blue")
P1 <- c(-3,2)
P2 <- c(1,-4)
Line <- CreateLinePoints(P1, P2)
Draw(Line, "black")
Poly_reflected <- ReflectedPolygon(Poly, Line)
Draw(Poly_reflected, "orange")
```

RemovePointPoly — *Removes a point from a previously defined polygon*

Description

RemovePointPoly creates a matrix to represent the polygon that connects several points

Usage

```
RemovePointPoly(Poly, position)
```

Arguments

Poly	Polygon object, previously created with function CreatePolygon or CreateRegularPolygon
position	Integer indicating the position of the point in the original polygon that is being removed. It is convenient to visualize the polygon with label = T in order to avoid mistakes

Value

Returns a matrix which contains the points of the polygon. Each row represents one of the points

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
n <- 5
C <- c(0,0)
l <- 2
Penta <- CreateRegularPolygon(n, C, l)
Penta <- RemovePointPoly(Penta, 4)
Draw(Penta, "blue", label = TRUE)
```

Rotate — *Rotates a geometric object*

Description

Rotate rotates a geometric object of any of the following types: line, polygon or segment

Usage

```
Rotate(object, fixed, angle)
```

Arguments

`object`	geometric object of type line, polygon or segment, previously created with any of the functions in the package
`fixed`	Vector containing the xy-coordinates of the only point of the plane which remains fixed during rotation
`angle`	Angle of rotation in degrees (0-360), considering the clockwise direction

Value

Returns a geometric object which is the rotation of the original one, following the clockwise direction

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
Draw(Poly, "blue")
fixed <- c(-1,-1)
angle <- 30
Poly_rotated <- Rotate(Poly, fixed, angle)
Draw(Poly_rotated, "orange")
fixed <- c(2,0)
Poly_rotated <- Rotate(Poly, fixed, angle)
Draw(Poly_rotated, "transparent")
```

`SelectPoints` *Selection of points from the coordinate plane*

Description

`SelectPoints` allows the selection of points from the coordinate plane

Usage

```
SelectPoints(n)
```

Arguments

`n`	Number of points to select from the current coordinate plane

Value

Returns a vector or matrix which contains the xy-coordinates of the selected points. Each row represents one of the points. If `n = 1` the output is a numeric vector, if `n = 2` then it is a `Segment`, and for `n > 2` the object is a polygon.

Examples

```
n <- 3
points <- SelectPoints(n)
```

`ShearedPolygon` *Creates a sheared polygon from a given one*

Description

`ShearedPolygon` creates a sheared polygon from a given one

Usage

```
ShearedPolygon(Poly, k, direction)
```

Arguments

`Poly`	Polygon object, previously created with function `CreatePolygon` or `CreateRegularPolygon`
`k`	Number that represents the shear factor which is applied to the original polygon
`direction`	String with value "horizontal" or "vertical" which indicates the direction in which shearing is applied. Horizontal means the shearing is parallel to the X axis, while vertical means parallel to the Y axis

Value

Returns a sheared polygon, in any of the two axis, to the original one

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
Square <- CreateRegularPolygon(4, c(-2, 0), 1)
Draw(Square, "blue")
k <- 1
Square_shearX <- Translate(ShearedPolygon(Square, k, "horizontal"), c(3,0))
Draw(Square_shearX, "orange")
Square_shearY <- Translate(ShearedPolygon(Square, k, "vertical"), c(3,0))
Draw(Square_shearY, "orange")
```

Sierpinski *Plots the Sierpinski triangle*

Description

Sierpinski plots the first iterations of Sierpinski triangle, a well-known fractal

Usage

```
Sierpinski(Tri, it)
```

Arguments

Tri	Regular triangle, previously created with function CreateRegularPolygon
it	Number of iterations to be performed for the construction of Sierpinski triangle. It is not recommended to choose a number higher than 10 in order to avoid an excess of computation

Value

None. It produces the plot of the first n iterations of Sierpinski triangle in the current coordinate plane

References

http://mathworld.wolfram.com/SierpinskiSieve.html

Examples

```
x_min <- -6
x_max <- 6
y_min <- -6
y_max <- 6
CoordinatePlane(x_min, x_max, y_min, y_max)
n <- 3
C <- c(0,0)
l <- 5
Tri <- CreateRegularPolygon(n, C, l)
it <- 6
Sierpinski(Tri, it)
```

SimilarPolygon *Creates a similar polygon to a given one*

Description

SimilarPolygon creates a sheared polygon from a given one

Usage

```
SimilarPolygon(Poly, k)
```

Arguments

Poly	Polygon object, previously created with function CreatePolygon or CreateRegularPolygon
k	Positive number that represents the expansion (k > 1) or contraction (k < 1) factor which is applied to the original polygon

Value

Returns a similar polygon, exapended or contracted, to the original polygon

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(0,0)
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
Draw(Poly, "blue")
k <- 2
Poly_similar <- SimilarPolygon(Poly, k)
Draw(Translate(Poly_similar, c(-1,2)), "orange")
```

Soddy *Finds the inner and outer Soddy circles of three given mutually tangent circles*

Description

Soddy finds inner and outer Soddy circles of three given mutually tangent circles

Usage

```
Soddy(A, r1, B, r2, C, r3)
```

Arguments

A	Vector containing the xy-coordinates of the center of circumference 1
r1	Radius for circumference 1
B	Vector containing the xy-coordinates of the center of circumference 2
r2	Radius for circumference 2
C	Vector containing the xy-coordinates of the center of circumference 3
r3	Radius for circumference 3

Value

A list which contains the Soddy center and the radiuses of Soddy inner and outer circle of three mutually tangent circles

References

http://mathworld.wolfram.com/SoddyCircles.html

Examples

```
x_min <- -3
x_max <- 3
y_min <- -2.5
y_max <- 3.5
CoordinatePlane(x_min, x_max, y_min, y_max)
A <- c(-1,0)
B <- c(1,0)
C <- c(0,sqrt(3))
r1 <- 1
r2 <- 1
r3 <- 1
Draw(CreateArcAngles(A, r1, 0, 360), "black")
Draw(CreateArcAngles(B, r2, 0, 360), "black")
Draw(CreateArcAngles(C, r3, 0, 360), "black")
result <- Soddy(A, r1, B, r2, C, r3)
soddy_point <- result[[1]]
inner_radius <- result[[2]]
outer_radius <- result[[3]]
Draw(soddy_point,"red")
Draw(CreateArcAngles(soddy_point,inner_radius,0,360),"red")
Draw(CreateArcAngles(soddy_point,outer_radius,0,360),"red")
```

`Star` *Creates a closed curve with the shape of a star. Each of the stars produced by this function is built through a simple iterative process based on segment drawing for certain angles and lengths. It can also produce regular polygons for some combinations of the parameters*

Description

`Star` creates a star with multiple building possibilities

Usage

```
Star(P, angle, l, time = 0, color = "transparent")
```

Arguments

`P`	Vector containing the xy-coordinates of the starting point for the star
`angle`	Angle (0-360) that is related to the direction of the two segments which are drawn in each of the steps of the process. This parameter really represents the angle (in clockwise and anti-clockwise direction) for the two first drawn segments, but it is modified according to rotations of 144 degrees in all the following steps, including the last one, which closes the curve.
`l`	Number that indicates the length side of the segments that are drawn. This parameter will determine the size of the star
`time`	Number of seconds to wait for the program before drawing each of the segments that make star. If no `time` is specified, default value is 0 (no waiting time). If the chosen time is very small (`time` < 0.05) it is possible that the program shows the plot directly. In this case, it should be increased the `time` parameter.
`color`	Color to indicate the points that are obtained during the process to draw the star. If missing, the points are not indicated and only the segments are drawn in the plot

Value

None. It produces the plot of a closed curve with the shape of a star, if the parameters are chosen properly

References

Abelson, H., & DiSessa, A. A. (1986). Turtle geometry: The computer as a medium for exploring mathematics. MIT press

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P <- c(0,0)
angle <- 0
l <- 1
Star(P, angle, l)
```

Tessellation *Creates a tessellation from a starting set of geometric objects*

Description

`Tessellation` creates a geometric pattern by the repetitive translation of an initial geometric object

Usage

```
Tessellation(objects_list, colors, direction, separation, it)
```

Arguments

`objects_list`	A list composed by several geometric objects (mainly polygons created with `CreatePolygon` or `CreateRegularPolygon`)
`colors`	Vector containing the colors for each of the objects of the initial geometric object
`direction`	Vector containing the xy-coordinates of the direction in which tessellation is being generated
`separation`	Number indicating the distance that separates any of the geometric objects in the repetitive pattern. This distance must be understood in the sense of a translation of the initial object. Indeed, this distance is only preserved in the direction of the chosen vector `direction` when generating the pattern. Moreover, the choice of `separation = 0` implies no pattern is generated
`it`	Number of iterations to be performed for the construction of the tessellation

Value

None. It produces the plot of a repetitive pattern, usually known as a tessellation

References

http://mathworld.wolfram.com/Tessellation.html

Examples

```
x_min <- -6
x_max <- 6
y_min <- -2
y_max <- 10
CoordinatePlane(x_min, x_max, y_min, y_max)
Hexa <- CreateRegularPolygon(6, c(-3,0), 1)
Draw(Hexa, "purple")
Tri <- CreatePolygon(c(-3,-1), c(Hexa[4,1],-2), c(Hexa[1,1],-2))
Draw(Tri,"pink")
objects_list <- list(Tri, Hexa)
cols <- c("pink", "purple")
direction <- c(1,0)
separation <- 1.732051
it <- 3
Tessellation(objects_list, cols, direction, separation, it)
direction <- c(0,1)
separation <- 3
it <- 4
Tessellation(objects_list, cols, direction, separation, it)
```

Translate — *Translates a geometric object*

Description

`Translate` translates a geometric object of any of the following types: line, polygon or segment

Usage

```
Translate(object, v)
```

Arguments

`object`	geometric object, previously created with function `CreatePolygon`
`v`	Vector containing the xy-coordinates of the translation vector

Value

Returns a polygon whose coordinates are translated according to vector `v`

Examples

```
x_min <- -5
x_max <- 5
y_min <- -5
y_max <- 5
CoordinatePlane(x_min, x_max, y_min, y_max)
P1 <- c(0,0)
```

```
P2 <- c(1,1)
P3 <- c(2,0)
Poly <- CreatePolygon(P1, P2, P3)
Draw(Poly, "blue")
v <- c(1,2)
Poly_translated <- Translate(Poly, v)
Draw(Poly_translated, "orange")
```

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